Thin films growth and deposition techniques

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Outlook

- 1. Introduction to thin films growth
- 2. Surface adsorption
- 3. Surface tension
- 4. Homogeneous nucleation
- 5. Heterogeneous nucleation
- 6. Strain effects
- 7. Growth modes
- 8. Coalescence processes
- 9. Deposition techniques
- 10.Evaporation

Credits:

Matteo Cantoni Slides of the Course on Micro and Nanofabrication held at Politecnico di Milano - Polifab



Introduction to thin films growth

How growth takes place?

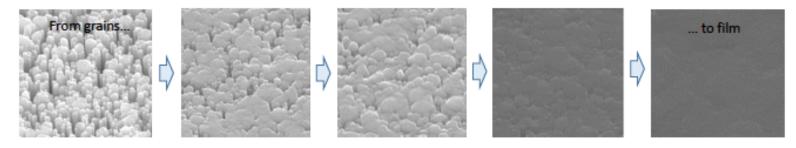
Condensation of atomic clusters on the substrate

Film thicknening due to additional deposition

Fully developed single-crystals (SC), polycrystals (PC) or amorphous films

Relationships between <u>film structure</u> and <u>growth process</u>

<u>Understanding</u> properties of the <u>deposited films</u>



Es. ZnO on sapphire (Al₂O₃)

Reference for this lecture: M. Ohring, Materials Science of Thin films, Academic Press, Chapters 1 and 7



Surfaces: adsorption reactions

What happens when a surface is exposed to gas particles?

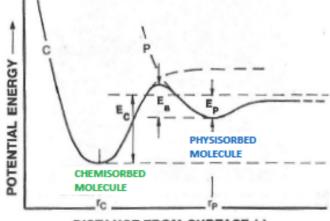
Surface adsorption – impinging atoms and molecules enter and interact within the transition region between the gas phase and the surface.

Physisorption (physical adsorption)
the particle is stretched or bent, but
retains its identity; van der Waals

forces bond it to the surface

Chemisorption (chemical adsorption)

the particle **changes its identity** through ionic or covalent bonding with surface atoms



DISTANCE FROM SURFACE (r)

Model of physisorption (P) and chemisorption (C) processes in terms of the interaction potential between adsorbate and surface vs. the distance from the surface (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 7)

Note that:

- r_p > r_C ⇒ P particles achieve equilibrium further from the surface than C ones
- E_P(~0.25eV) << E_C (~1-10eV) ⇒ very different adsorption heats (or energies)
- Dissociation: dissociative chemisorption is possible if E_{dis} < E_C
- When both P and C occur, the transition rate from P to C is governed by the effective energy E_a
- In the following we will use a composite energy of adsorption (integrated over all adsorption states) E_{ads}, and correspondingly a composite energy of desorption (integrated over all desorption states) E_{des}



Surfaces: adsorption effects (1)

How the surface adsorption and desorption energies influence film growth?

- Consider a <u>vapor phase</u> containing adatoms at <u>partial pressure P</u>, that will <u>condensate</u> on a <u>substrate surface</u> (or the surface
 of a film previously grown, with the same hypotesis of cleanliness and sharpness)
- The net time rate of the substrate coverage θ is given by:

$$\frac{d\theta}{dt} = k_{ads} P(1-\theta) - k_{des} \theta$$

where:

- θ = 0 means no coverage, θ = 1 means one monolayer (1 ML) coverage
- The first term is the <u>rate of adatoms coverage at the unoccupied surface</u> sites (1-θ); it is proportional to the partial pressure P and the <u>absorption rate</u> constant, that depends on the composite <u>adsorption energy</u> as:

$$k_{ads} \sim \exp(-E_{ads}/k_BT) \implies k_{ads}$$
 increases when E_{ads} decreases

The second term is the <u>rate of adatoms desorption from the occupied surface sites</u> (θ); it is proportional to the desorption rate constant, that depends on the composite desorption energy as:

$$k_{des} \sim \exp(-E_{des}/k_BT)$$
 $\Longrightarrow k_{des}$ decreases when E_{des} increases



Surfaces: adsorption effects (2)

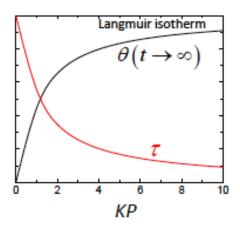
$$\frac{d\theta}{dt} = k_{ads}P(1-\theta) - k_{des}\theta \implies \text{The solution is: } \\ \theta(t) = \frac{KP}{1+KP} \Big[1-\exp\big(-k_{des}(1+KP)t\big)\Big] \text{, with } K = k_{ads}/k_{des}$$

Note that:

- If
$$t \to \infty$$
 (or $t >> \tau$, with $\tau = \left[k_{des}(1 + KP)\right]^{-1}$) $\Longrightarrow \theta(t) \approx \frac{KP}{1 + KP}$ (Langmuir isotherm)

- If KP>>1 \longrightarrow $\{\theta(t)\approx 1 \text{ (the surface is covered by one monolayer of adatoms)}$ $\tau\approx \left[k_{des}KP\right]^{-1}=\left[k_{ads}P\right]^{-1}\to 0$

(
$$KP = \frac{k_{ads}}{k_{des}}P >> 1$$
 means large P and/or $k_{ads} >> k_{des}$)
($E_{ads} << E_{des}$)





Thermodynamics aspects of nucleation

Electronics Structure Adsorption Roughening

atomistic details of the surface microscopic view



Thermodynamics aspects of nucleation G (Gibbs free energy)

- Nucleation involves the creation a new phase, with generally different structure and/or composition (es. a solid phase), from a previously stable phase (es. a vapor phase) when critical boundaries between stable phase fields in equilibrium phase diagram are crossed (e.g. by decreasing the temperature, triggering the condensation process).
- Nucleation occurs during the very early stages of phase change, but have a strong influence on the grain structure that ultimately develops in a deposition process.
- Nucleation concerns the formation a single stable nucleus
- Homogenous nucleation is the easiest case: the formation a solid nucleus from a prior supersaturated vapor

Questions:

- Under which conditions nuclei of films deposited are thermodynamically stable?
- What is the role of surface energy in film nucleation?
- How large nuclei are?
- What is the energy barrier to be surmounted in their formation?
- Which is the growth mode (island, planar, S-K)?
- How deposition rate and temperature influence nucleation energetics and size?



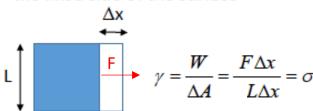
Surface energies

Capillarity (or droplet) theory of homogenous nucleation:

- A solid (S) nucleates from a prior instable liquid (L) or vapor (V) phase by establishing a S-L or S-V interface.
- Interfacial (or surface) free energies γ are associated to the interface (or surface).
- They quantify the disruption of intermolecular bonds that occur when a surface is created. Surfaces are intrinsically less energetically favorable than the bulk of a material (the molecules on the surface have more energy compared with the molecules in the bulk of the material), otherwise there would be a driving force for surfaces to be created, removing the bulk of the material. The surface energy may therefore be defined as the excess energy at the surface of a material compared to the bulk, or the work required to build an area of a particular surface.

Material	γ (J/m2)
Glass	0.37
NaCl	0.40
Al	1.15
MgO	1.20
Si	1.24
Au	1.50
Cu	1.81
П	2.00
Ni	2.41
Fe	2.45
Pt	2.48
Co	2.53
Cr	3.32

- Surface energy is defined as $\gamma=W/\Delta A$, where W is the reversible work done on a material for increasing its surface area by ΔA .
- Surface tension (σ) is defined as $\sigma = F/L$ where F is the force counteracting the surface increase and L is the fixed side of the surface





Homogeneous nucleation (1)

Homogeneous nucleation of a **spherical solid** phase of radius *r* from a supersaturated **vapor**:

- The gas-to-solid transformation modifies the chemical free energy of the system of $\frac{4}{3}\pi r^3\Delta G_{V}$
 - $\triangleright \Delta G_V$ is the chemical free energy change per unit volume
 - For the condensation reaction V \rightarrow S, ΔG_V is given by $\Delta G_V = -\frac{k_B T}{\Omega} \ln \frac{P_V}{P_S}$, where P_S and P_V are the vapor pressure above the solid and of the supersaturated vapor, respectively, and Ω is the atomic volume
 - $P_V > P_S$ for a supersaturated vapor (a supersaturated vapor of a compound is characterized by an higher partial pressure than the vapor pressure of the compound) $\Rightarrow \Delta G_V < 0 \Rightarrow$ nucleation takes place because the free energy of the system reduces
- Simultaneously, new surfaces or interfaces form \Rightarrow the surface free energy of the systems increases by $4\pi r^2 \gamma$, where γ is the S-V interfacial energy per unit area.
- The total free energy change in forming the nucleus is

$$\Delta G = \frac{4}{3}\pi r^3 \Delta G_V + 4\pi r^2 \gamma$$

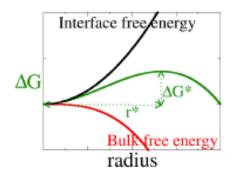


Homogeneous nucleation (2)

Homogeneous nucleation of a **spherical solid** phase of radius *r* from a supersaturated **vapor**:

Looking at the stationary point of ΔG leads to the equilibrium radius size:

$$\Delta G = \underbrace{\frac{4}{3}\pi r^3 \Delta G_v}_{\text{Surface/interface > 0}} + \underbrace{\frac{d\Delta G}{dr}}_{\text{Surface/interface > 0}} + \underbrace{\frac{d\Delta$$



 ΔG^* represents the energy barrier to the nucleation process:

- If a spherical cluster with radius $r < r^*$ forms by thermodynamical fluctuations, it is unstable and will shrink by losing atoms (reducing r for reducing ΔG)
- Cluster with radius r>r* have surmounted the nucleation energy barrier ΔG* and are stable. They tend to further grow (increasing r for reducing ΔG)

Homogeneous nucleation (3)

Homogeneous nucleation of a **spherical solid** phase of radius *r* from a supersaturated **vapor**:

Nucleation rate:
$$\frac{dN}{dt} = N * A * \omega$$
, with:

- N^* =equilibrium concentration (per cm³) of stable nuclei (proportional to the Boltzmann factor) = $n_S \exp(-\Delta G */k_B T)$
 - $n_{\rm S}$ =density of all possible nucleation sites (nuclei/cm³), $\Delta G^* = \frac{16\pi\gamma^3}{3\Delta G_v^2}$
- A^* =critical area (cross section) for each nucleus (cm²) = $4\pi r^2$
- ω = impingement atoms rate (atoms/cm²s) = $\alpha \frac{N_A (P_V P_S)}{(2\pi MRT)^{1/2}}$ ($\phi = N_A P/(2\pi MRT)^{1/2}$ was the gas impingement flux in a chamber of pressure P, see Lecture #2)
 - α = sticking coefficient (0-1)
 - M=atomic weight

$$\frac{dN}{dt} = n_S \exp\left(-\frac{\Delta G^*}{k_B T}\right) \frac{4\pi r^2}{\left(2\pi MRT\right)^{1/2}}$$

Note: the nucleation rate is mostly influenced by the exponential term, that is function of ΔG^* and thus of P_V/P_S (through ΔG_V):

$$P_V/P_S$$
 larger $\Rightarrow \Delta G_V^2 = \left(\frac{k_B T}{\Omega} \ln \frac{P_V}{P_S}\right)^2$ larger $\Rightarrow \Delta G^*, r^*$ smaller \Rightarrow {nucleation is possible (smaller energy barrier and critical size)} the nucleation rate is larger



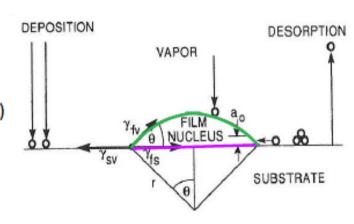
Capillarity theory of heterogeneous nucleation (1)

Heterogeneous nucleation of a condensed film on a substrate:

- We extend the capillarity theory of <u>homogeneous</u> nucleation (condensation from a vapor phase of a <u>single</u> chemical species used only in some CVD processes) to a condensed film on a substrate → we have two species (substrate and depositing material) and two phases (the depositing material is both in solid the film and vapor phases)
 - capillarity theory of <u>heterogeneous</u> nucleation
- Atoms or molecules in the vapor phase impinge on the substrate creating nuclei of mean dimension r.
- The free-energy change accompanying the formation of such nuclei is given by

$$\Delta G = a_3 r^3 \Delta G_V + a_1 r^2 \gamma_{fV} + a_2 r^2 \gamma_{fS} - a_2 r^2 \gamma_{SV}$$

- ΔG_V is the chemical free energy change per unit volume that drives the condensation reaction (as in homogenous nucleation)
- γ are the interfacial tensions between film (f), substrate (S) and vapor (V)
- a₁r² is the curved surface area (interface f-V)
- a_2r^2 is the projected area on the substrate (interface f-S)
- a₃r³ is the film volume



Schematic of basic nucleation processes on substrate during vapor deposition (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 7)



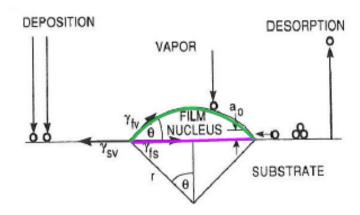
Capillarity theory of heterogeneous nucleation (2)

$$\Delta G = a_3 r^3 \Delta G_V + a_1 r^2 v_{fV} + a_2 r^2 v_{fS} - a_2 r^2 v_{SV}$$

- ΔG_V is the chemical free energy change per unit volume
- y are the interfacial tensions between film (f), substrate (S) and vapor (V)
- a₁r² is the curved surface area (interface f-V)
- a₂r² is the projected area on the substrate (interface f-S)
- a₃r³ is the film volume

For the spherical cap-shaped solid nucleus in figure:

$$a_1 = 2\pi (1 - \cos \theta), a_2 = \pi \sin^2 \theta, a_3 = \pi/3 (2 - 3\cos \theta + \cos^3 \theta)$$



Schematic of basic nucleation processes on substrate during vapor deposition (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 7)

Note: when a new interface appears:

- the surface energy of the film increases (+ sign for the first two surface/interface terms, f-V and f-S)
- the reduction of the S-V interface under the cap implies a reduction in the system energy (- sign for the last interface terms, S-V)

Mechanical equilibrium in the horizontal (parallel to substrate) direction:

$$-\gamma_{SV} + \gamma_{fS} + \gamma_{fV} \cos \theta = 0$$

$$\cos \theta = \frac{\gamma_{SV} - \gamma_{fS}}{\gamma_{fV}}$$

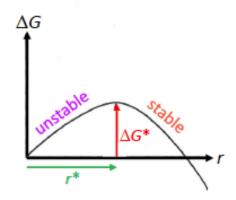
The wetting angle θ depends only on the material properties (the interface tensions)

Capillarity theory of heterogeneous nucleation (3)

$$\Delta G = a_3 r^3 \Delta G_V + a_1 r^2 \gamma_{fV} + a_2 r^2 \gamma_{fS} - a_2 r^2 \gamma_{SV}$$

Looking at the stationary point of ΔG leads to the equilibrium radius size:

$$\begin{split} \frac{d\Delta G}{dr} &= 3a_{3}r^{2}\Delta G_{V} + 2a_{1}r\gamma_{fV} + 2a_{2}r\gamma_{fS} - 2a_{2}r\gamma_{SV} = r\left(3a_{3}\Delta G_{V}r + 2\left(a_{1}\gamma_{fV} + a_{2}\gamma_{fS} - a_{2}\gamma_{SV}\right)\right) = 0 \\ \Rightarrow \begin{cases} r^{*} &= -\frac{2\left(a_{1}\gamma_{fV} + a_{2}\gamma_{fS} - a_{2}\gamma_{SV}\right)}{3a_{3}\Delta G_{V}} \\ \Delta G^{*} &= \frac{4\left(a_{1}\gamma_{fV} + a_{2}\gamma_{fS} - a_{2}\gamma_{SV}\right)^{3}}{27a_{3}^{2}\Delta G_{V}^{2}} \end{split}$$



Heterogeneous nucleation behaves as homogeneous nucleation:

- r^* is the critical nucleus size and ΔG^* is the critical free energy barrier for nucleation.
- Nuclei are unstable for r<r* (they disappear by shrinkig, lowering ΔG), and stable for r>r* (they grow to supercritical dimensions by addition of atoms, lowering ΔG)



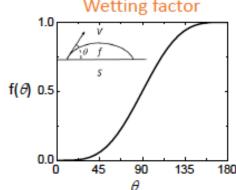
Capillarity theory of heterogeneous nucleation (4)

For the spherical cap-shaped solid nucleus:

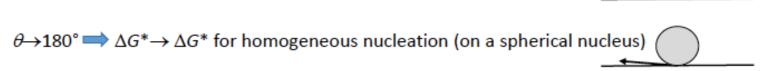
$$a_1 = 2\pi (1 - \cos \theta), a_2 = \pi \sin^2 \theta, a_3 = \pi/3 (2 - 3\cos \theta + \cos^3 \theta)$$

Using the mechanical equilibrium condition parallel to substrate ($-\gamma_{SV} + \gamma_{fS} + \gamma_{fV} \cos \theta = 0$) we obtain:

$$\Delta G^* = \frac{4\left(2\pi\left(1-\cos\theta\right)\gamma_{fV} + \pi\sin^2\theta\left(\gamma_{fS} - \gamma_{SV}\right)\right)^3}{3\pi^2\left(2-3\cos\theta + \cos^3\theta\right)^2\Delta G_V^2} = \frac{4\left(2\pi\left(1-\cos\theta\right)\gamma_{fV} - \pi\sin^2\theta\gamma_{fV}\cos\theta\right)^3}{3\pi^2\left(2-3\cos\theta + \cos^3\theta\right)^2\Delta G_V^2} = \frac{16\pi\gamma_{fV}^3}{3\Delta G_V^2} \underbrace{\left(2-3\cos\theta + \cos^3\theta\right)^2\Delta G_V^2} = \underbrace{\left(2\pi\left(1-\cos\theta\right)\gamma_{fV} - \pi\sin^2\theta\gamma_{fV}\cos\theta\right)^3}_{\Delta G^* \text{ for } Function \text{ of the homogeneous contact (wetting)}}_{\Delta G^* \text{ for } G^$$



 $\theta \rightarrow 0 \implies \Delta G^* \rightarrow 0$: when the film wets the substrate, there is **no barrier** for nucleation





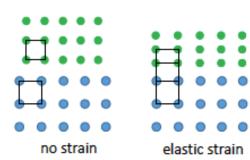
Capillarity theory of heterogeneous nucleation (5)

Other energy contributions (e.g. elastic strain) can be easily included in the free energy change expression:

$$\Delta G = a_3 r^3 \Delta G_V + a_1 r^2 \gamma_{fV} + a_2 r^2 \gamma_{fS} - a_2 r^2 \gamma_{SV} + a_3 r^3 \Delta G_S$$

 $\Delta G_{\rm S}$ is the strain free-energy change per unit volume. It arises, e.g., from elastic strain of the film because of bonding mismatch between film and substrate.

$$\Delta G^* = \frac{4\left(a_1\gamma_{fV} + a_2\gamma_{fS} - a_2\gamma_{SV}\right)^3}{27a_3^2\left(\Delta G_V + \Delta G_S\right)^2}$$



Note:

- $\Delta G_V < 0 \Rightarrow \text{if } \Delta G_S > 0$ (as in the figure) the energy barrier for nucleation ΔG^* will increase
- However if ΔG_s <0 (e.g. because of stress relieval during nucleation on an *initially strained substrate*) the energy barrier for nucleation ΔG^* will decrease and thus nucleation will be favoured
- ΔG* could also be affected by substrate charge and impurities, affecting surface and/or volume electrostatic, chemical, etc., energy contributions ⇒ they can be treated in the same framework

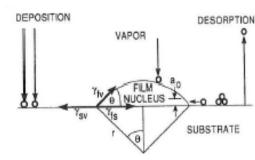


Film growth modes (1)

Mechanical equilibrium in the horizontal (parallel to substrate) direction:

$$-\gamma_{sv} + \gamma_{fs} + \gamma_{fv} \cos \theta = 0 \quad \text{(Young's equation)} \quad \Longrightarrow \quad \cos \theta = \frac{\gamma_{sv} - \gamma_{fs}}{\gamma_{fv}}$$

The wetting angle θ depends only on the material properties (the interface tensions γ_{SV} , γ_{fS} , γ_{fV})



Schematic of basic nucleation processes on substrate during vapor deposition (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 7)

- Island growth:
$$\theta > 0$$
 \Longrightarrow $\cos \theta = \frac{\gamma_{SV} - \gamma_{fS}}{\gamma_{fV}} < 1$ \Longrightarrow $\gamma_{SV} - \gamma_{fS} < \gamma_{fV}$ \Longrightarrow $\gamma_{SV} < \gamma_{fS} + \gamma_{fV}$

Note: if we neglect γ_{fS} , island growth occurs when the surface tension of the film γ_{fV} exceeds that of the substrate γ_{SV} \Rightarrow leaving the substrate uncovered leads to energy minimization

E.g.: $\gamma_{fV} = 1.50 \text{ J/m}^2$ for Au, $\gamma_{SV} = 0.86 \text{ J/m}^2$ for GaAs(110) \Rightarrow in general, deposited metals tend to cluster on substrates

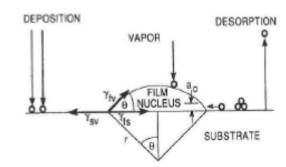
- Layer growth:
$$\theta \approx 0$$
 \implies $\cos \theta = \frac{\gamma_{SV} - \gamma_{fS}}{\gamma_{fV}} = 1$ \implies $\gamma_{SV} - \gamma_{fS} = (\geq)\gamma_{fV}$ \implies $\gamma_{SV} \geq \gamma_{fS} + \gamma_{fV}$



Film growth modes (2)

- Island growth: θ > 0 $\Rightarrow \gamma_{SV} - \gamma_{fS} < \gamma_{fV} \Rightarrow \gamma_{SV} < \gamma_{fS} + \gamma_{fV}$

- Layer growth:
$$\theta \approx 0$$
 $\Longrightarrow \gamma_{SV} - \gamma_{fS} = (\geq) \gamma_{fV} \Longrightarrow \gamma_{SV} \geq \gamma_{fS} + \gamma_{fV}$



<u>Note#1</u>: homo-epitaxy (or auto-epitaxy): $\gamma_{fS} = 0$ (it is a special case of the layer growth condition in which the interface between film and substrate essentially vanishes)

<u>Note#2</u>: high-quality epitaxial growth of films requires **continuity during the growth** (no disruption to layer growth) $\Rightarrow \gamma_{f5} = 0$ because film (or overlayer to be grown) and substrate (or underlayer already grown) are the same

Note#3: consider a superlattice composed of alternating stacked A and B epitaxial films



- if the surface energies γ_{fV} and γ_{SV} are similar (e.g. for semiconductor-semiconductor) the superlattice can be **epitaxial** too (we assume to neglect γ_{fS})
- if the surface energies γ_{fV} and γ_{SV} are different (e.g. for metal-metal or metal-semiconductor) epitaxy is not guaranteed
 - materials with low γ will wet substrates with large γ ($\gamma_{fV} < \gamma_{SV}$)
 - materials with large γ will clusterize on substrates with low γ ($\gamma_{fV} > \gamma_{SV}$)



Morphological stability of strained layers (1)

How to address quantitatively strain at an interface between layers?

- From elasticity theory the strain free energy per unit volume (E_S) can be expressed as

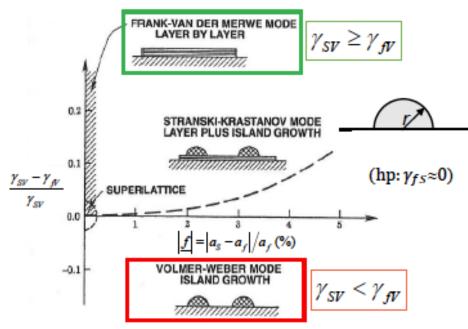
$$= \frac{1}{2} Y \varepsilon^2 h A$$

where Y is the elastic modulus of the film and ε is the strain.

- The strain ε at the interface can be measured as the lattice mismatch strain (or misfit) defined as

$$\underline{f} = \frac{a_{s} - a_{f}}{a_{f}}$$

where a_s and a_f are the lattice parameters of the upper layer (e.g., the film) and the lower layer (e.g., the substrate), respectively.



Stability regions of the three film growth modes in coordinates of surface enery difference between film and substrate (y-axis) and lattice misfit (x-axis) (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 7)

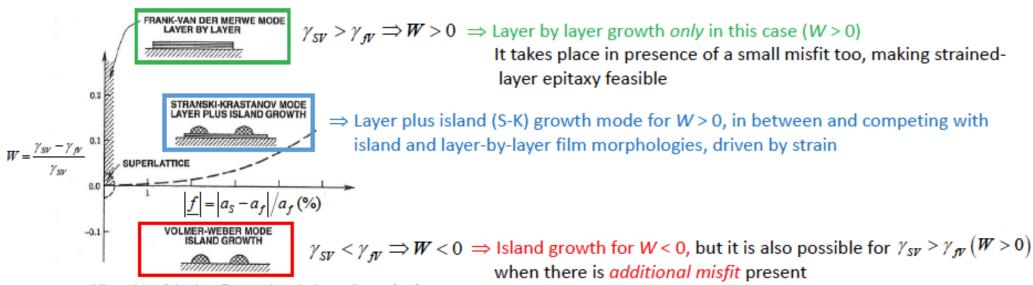
Which is the critical film thickness beyond which a strained planar film roughens due to the growth of islands?

$$h^* = \frac{2\gamma_{fS}}{Y(\varepsilon^2 - \underline{f}^2)}$$

- ε is the mean misfit in the strained epilayer after nucleation, that minimizes the total energy by partially relaxing
- <u>f</u> is the misfit of the epilayer <u>prior</u> to nucleation, due to the misfit with the substrate



Morphological stability of strained layers (5)



Stability regions of the three film growth modes in coordinates of surface enery difference between film and substrate (y-axis) and lattice misfit (x-axis) (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 7)



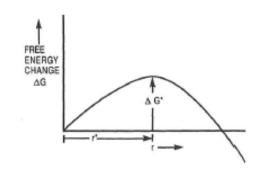
Nucleation dependence on temperature

How substrate temperature and deposition rate influence the deposition process?

• Assuming an inert substrate (that is not reacting with the vapor phase) with $\gamma_{fV} = \gamma_{fS}$ and $\gamma_{VS} = 0$ we have (see slide 20):

$$r^* = -\frac{2(a_1 \gamma_{fV} + a_2 \gamma_{fS} - a_2 \gamma_{SV})}{3a_3 \Delta G_V} = -\frac{2(a_1 + a_2) \gamma_{fV}}{3a_3 \Delta G_V}$$

$$\Rightarrow \frac{\partial r^*}{\partial T}\Big|_{\dot{R}} = -\frac{2}{3} \left(a_1 + a_2\right) \frac{\frac{\partial \gamma_{fV}}{\partial T} a_3 \Delta G_V - \gamma_{fV} a_3}{\left(a_3 \Delta G_V\right)^2} = \frac{2}{3} \left(a_1 + a_2\right) \frac{\gamma_{fV}}{\partial T} \frac{\frac{\partial \Delta G_V}{\partial T} - \Delta G_V}{\partial T} \frac{\frac{\partial \gamma_{fV}}{\partial T}}{\partial T}$$



Free energy change (ΔG) as a function of radius (r). (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 1)

- •Assuming typical values we have $\frac{\partial r^*}{\partial T}\Big|_{R} > 0$
- Moreover, we also have $\frac{\partial \Delta G^*}{\partial T}\Big|_{R} > 0$



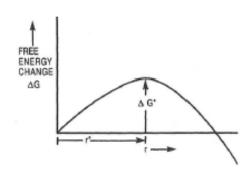
Nucleation dependence on deposition rate

How substrate temperature and deposition rate influence the deposition process?

- ΔG_v is the chemical free energy change per unit volume (see slide 15)
- For the condensation reaction V \rightarrow S, ΔG_V is given by $\Delta G_V = -\frac{k_BT}{\Omega} \ln \frac{P_V}{P_S}$, where P_S and P_V are the vapor pressure above the solid and of the supersaturated vapor, respectively, and Ω is the atomic volume
- Assuming the deposition rate \dot{R} (atoms/cm²s) on the film nucleus proportional to $P_{\rm V}$ and the equilibrium evaporation rate \dot{R}_e (from the film nucleus at the substrate temperature) proportional to $P_{\rm S}$, we have $\Delta G_{\rm V} = -\frac{k_BT}{\Omega} \ln \frac{\dot{R}}{\dot{R}_e}$

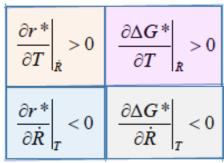
$$\frac{\partial r^*}{\partial \dot{R}}\Big|_{T} = \frac{\partial r^*}{\partial \Delta G_{V}}\Big|_{T} \frac{\partial \Delta G_{V}}{\partial \dot{R}}\Big|_{T} = \frac{\partial \left[-\frac{2(a_{1} + a_{2})\gamma_{fV}}{3a_{3}\Delta G_{V}}\right]}{\partial \Delta G_{V}} \frac{\partial \left[-\frac{k_{B}T}{\Omega}\ln\frac{\dot{R}}{\dot{R}_{e}}\right]}{\partial \dot{R}} = \frac{r^*}{\Delta G_{V}} \frac{k_{B}T}{\Omega \dot{R}}$$

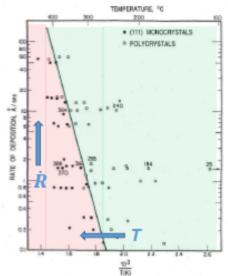
- Because $\Delta G_V < 0$, we have $\frac{\partial r^*}{\partial \dot{R}}\Big|_T < 0$
- Moreover, we also have $\frac{\partial \Delta G^*}{\partial \dot{R}}\Big|_{T} < 0$



Free energy change (ΔG) as a function of radius (r). (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 1)

Nucleation dependence on temperature and deposition rate





Some observation on common effects observed in thin films deposition:

- Higher T leads to higher critical radius $r^* \Rightarrow$ an island structure persists to an higher coverage
- A nucleation barrier may exist at higher substrate T, while at lower T it is reduced in magnitude
- Because N^* (the equilibrium concentration of stable nuclei, see slide 17) exponentially depends on ΔG^* ($\propto \exp(-\Delta G^*/k_BT)$), the number of supercritical nuclei decreases rapidly with $T \Rightarrow$ a continuous film will take longer to develop
- Increasing the deposition rate \dot{R} results in smaller islands (smaller r^*)
- Increasing the deposition rate \dot{R} also reduces the nucleation barrier (smaller ΔG^*), favouring continuous films at lower average film thickness

We associate:

- Large r^* and ΔG^* to large crystallite or even monocrystals \implies favoured by high T and low R
- Small r^* and ΔG^* to polycrystalline films \implies favoured by low T and high R

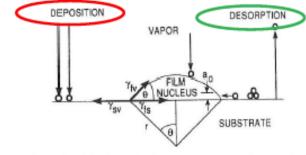
Dependence of microstructure on deposition rate \dot{R} and substrate temperature τ for Cu films on NaCl(111) (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 1)



Nucleation rate (1)

How many nuclei of critical size form on the substrate per unit area and time?

- The rate at which critical nuclei grow depends on the rate at which adsorbed monomers (adatoms) attach to it.
- Energetic vapor atoms which impinge on the substrate usually remain on the surface for a length time τ_s before desorbing:



Schematic of basic nucleation processes on substrate during vapor deposition (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 7)

$$\tau_S = \frac{1}{\nu} \exp\left(\frac{E_{des}}{k_B T}\right)$$

where ν is the vibrational frequency of an adatom on the surface ($\sim 10^{13}$ s⁻¹) and E_{des} is the energy required to desorb it back into the vapor.

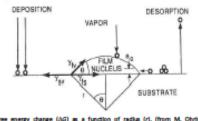
- Adatoms not yet accommodated to the substrate, executing random diffusive jumps, can form stable pairs with other adatoms or attach to larger atomic clusters or nuclei (it is unlikely that further return to the vapor phase)
- This typically happens at substrate heterogeneities (cleavage steps, edges, imperfections) where the binding energy of
 adatoms is larger than in a planar surface ⇒ the larger number of atomic bonds at this sites leads to higher E_{des}.



Nucleation rate (2)

Nucleation rate:
$$\frac{dN}{dt} = N * A * \omega$$
 (nuclei/cm²s) with:

- N*=equilibrium concentration (per cm²) of stable nuclei (proportional to the Boltzmann factor)
- A^* =critical area (cross section) for each nucleus (cm²) = $2\pi r^* a_0 \sin \theta$
- ω = impingement atoms rate (atoms/cm²s) onto nuclei with critical area A*



Free energy change (AG) as a function of radius (r). (from M. Oh Materials Science of Thin films, Academic Press, Chapter 1)

- Of the total nucleation site density, only n_a will be occupied by adatoms: $n_a = \phi \tau_S = \frac{\tau_S N_A P}{\left(2\pi MRT\right)^{1/2}}$ $\phi = N_A P/\left(2\pi MRT\right)^{1/2}$ is the vapor impingement flux in a chamber of pressure P, see Lesson #2 $\tau_S = \frac{1}{\nu} \exp\left(\frac{E_{des}}{k_* T}\right)$ is the adatom lifetime on the substrate (between adsorption and desorption)
- Atoms that have not yet thermally accommodated to the substrate execute random diffusive jumps, ending up to
 accommodate in clusters or nuclei. After this accommodation, desorption becomes an unlikely process. The impingment rate
 onto area A* thus considers diffusive jumps on the substrate, with a frequency given by

$$v \exp\left(-\frac{E_s}{k_B T}\right)$$
 , where E_s is the activation energy for surface diffusion.

The overall impingement flux is thus $\omega = n_a v \exp\left(-\frac{E_s}{k_B T}\right) = \frac{\tau_s N_A P}{\left(2\pi MRT\right)^{1/2}} v \exp\left(-\frac{E_s}{k_B T}\right)$ (nuclei/cm²s)



Nucleation rate (3)

Residence time prior to re-evaporation

Finally we obtain the nucleation rate:

$$\frac{dN}{dt} = N * A * \omega = n_S \exp\left(-\frac{\Delta G}{k_B T}\right) 2\pi r * a_0 \sin\theta \frac{1}{v} \exp\left(\frac{E_{des}}{k_B T}\right) N_A P \left(\frac{E_{des}}{k_B T}\right) \exp\left(-\frac{E_S}{k_B T}\right) = 0$$
Diffusion frequency on the substrate

$$=2\pi r^* a_0 \sin \theta \frac{PN_A}{\left(2\pi MRT\right)^{1/2}} n_S \exp \left(\frac{E_{des} - E_S - \Delta G^*}{k_B T}\right)$$

Note:

- The nucleation rate exponentially depends on the nucleation energetics via ΔG^* ($\propto \exp(-\Delta G^*/k_BT)$ that is **proportional to N*** (the equilibrium concentration of stable nuclei)
- The nucleation rate is proportional to the vapor pressure P
- The nucleation rate depends on T mainly via the exponential factor POSITIVE OR NEGATIVE? TO CHECK the rate decreases monothonically with T



Cluster coalescence and depletion

What happens to the density of stable nuclei in time?

- First, it increases with time up to some maximum level...
- ... then it decreases because of coalescence phenomena.

During growth and coalescence it typically happens that

- the total projected area of nuclei on the substrate decreases
 - the heigth of the surviving clusters increases
- nuclei with defined crystallographic facets initially become rounded...
- ... whereas composite islands reassume a crystallographic shape with time
- when two islands with different crystal structure coalesce, the final composite island assumes the crystallographic orientation of the larger one
- the coalescence process appears to be liquid-like, with islands merging and changing shape following a liquid
 droplet motion model
 - Before impacting and merging, cluster migrate over the substrate surface (cluster-mobility coalescence)

Coalescence mechanisms:

- Ostwald ripening
- Cluster migration
- Sintering

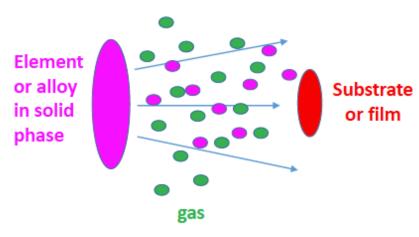


Introduction to deposition techniques

Objective of deposition techniques:

To controllably transfer atoms from a source to a target

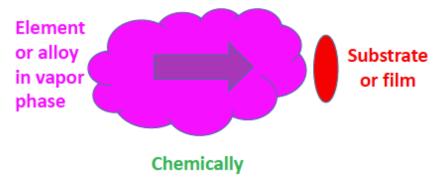
How the material is transferred from the source to the target?



Physically

The source material is physically transferred from a condensed phase evaporant to the target substrate

Physical vapor deposition (PVD)



A volatile compound of the material to be deposited chemically reacts with other gases to produce a nonvolatile solid that deposits atomistically on the target substrate

Chemical vapor deposition (CVD)



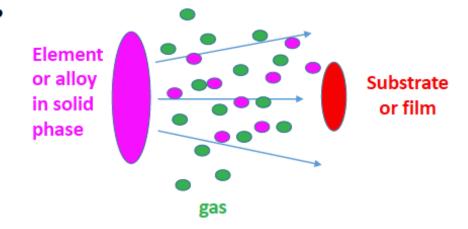
Introduction to PVD tecniques

How the material is transferred from the source to the target?

Physically

The source material is physically transferred from a condensed phase evaporant to the target substrate

Physical vapor deposition (PVD)



Which is the **physical** mechanism for transferring the material from the **source** to the **target**?

➤ evaporation caused by absorption of thermal energy (liquid or solid targets) → lecture 5

Which is the mechanism providing thermal energy to source atoms? Electrical heating, electron beam, pulsed laser,...

- ➤ sputtering by bombarding solid surfaces with energetic ions → lecture 6
- \triangleright In all cases the emitted atoms traverse a high vacuum region before to deposit on the target \rightarrow lecture 2



Evaporation rate

Hertz-Knudsen, 1882:

- 1. a liquid has a specific ability to evaporate at a given temperature;
- 2. the evaporation rate is proportional to the difference between the equilibrium pressure of the evaporant (P_e) and the hydrostatic pressure acting on it (P_h)
- The evaporation rate from liquid and solid sources is given by $\phi_s = \frac{\alpha_s N_A (P_s P_h)}{(2\pi MRT)^{1/2}}$

where ϕ_e is the evaporation flux (molecules/cm²s) and α_e is the coefficient of evaporation (0-1).

Note: the other parameters (M,R,T) and their dependences are equivalent to the gas impingement flux equation, see Lecture 2: $\phi = N_A P/(2\pi MRT)^{1/2}$

The maximum evaporation rate is attained when α_e =1 and P_h =0 (high vacuum or UHV is needed): $\phi_e = \frac{N_A P_e}{\left(2\pi MRT\right)^{1/2}}$

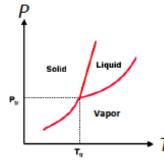
The mass evaporation rate instead is
$$\Gamma_e(\text{g/cm}^2\text{s}) = \phi_e \frac{M}{N_A} = 5.84 \cdot 10^{-2} \left(\frac{M}{T}\right)^{1/2} P_e(\text{torr})$$

Note: the evaporation rate strongly depends on T, both through the $T^{-1/2}$ dependence and because it deeply influences the equilibrium pressure P_e



Vapor pressure (1)

Clausius-Clapeyron equation for <u>solid-vapor</u> and <u>liquid-vapor</u> equilibria: $\frac{dP}{dT} = \frac{\Delta H}{T\Delta V}$

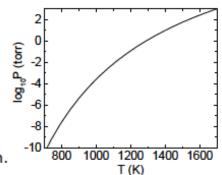


- ΔH and ΔV refer to the difference between the vapor and the condensed (solid or liquid) phases, whereas T is the transition temperature (the two phases are in equilibrium and coexist)
- $\Delta V = V_{Vapor} V_{condensed} \approx V_{vapor}$ because typically $V_{Vapor} >> V_{condensed}$
- Considering the vapor as a perfect gas, we have $V_{vapor}=RT/P$ (for 1 mol)

- $\Rightarrow \frac{dP}{dT} = \frac{P\Delta H_e}{RT^2}$
- In general $\Delta H = \Delta H(T)$, but as a first approximation we assume $\Delta H = \Delta H_e$, the molar heat of evaporation

$$\frac{dP}{P} = \frac{\Delta H_e}{R} \frac{dT}{T^2} \implies \ln \frac{P}{P_0} = -\frac{\Delta H_e}{RT} \implies \ln P = -\frac{\Delta H_e}{RT} + \ln P_0$$

$$P(T) = P_0 \exp\left(-\frac{\Delta H_e}{RT}\right)$$



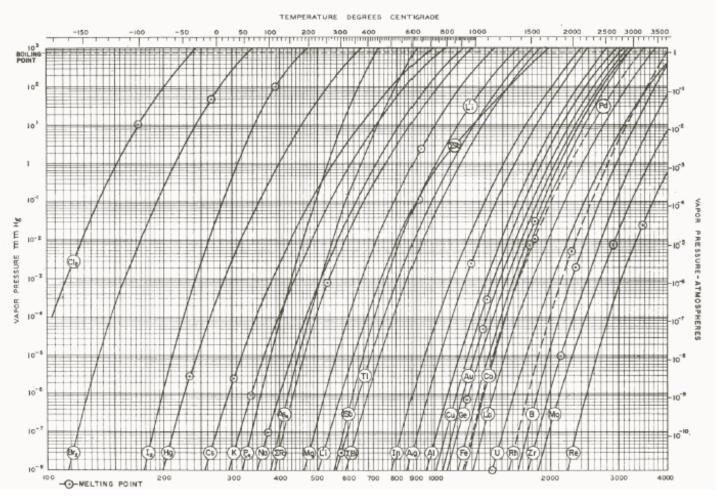
- P_0 is a constant that can be determined using the boiling point: $\Delta H_e = \Delta H_V$ (the latent heat of vaporization), T=boiling temperature, P=1 atm.

Note: this equation (Arrhenius-type law) holds for small temperature ranges, otherwise the $\Delta H(T)$ dependence must be considered. E.g., for the vapor pressure of liquid a better approximation is

$$\log P \text{ (torr)} = -15.993/\text{T} + 12.409 - 0.999 \log T - 3.52 \cdot 10^{-6} T$$

- Experimental vapor pressures (the pressure at which vapor and solid/liquid phases are in equilibrium and coexist) of the more common elements.
- Dots represent the melting points.
- The intercept with the horizontal dashed line correspond to the boiling points at ambient pressure.

Vapor pressure (2)

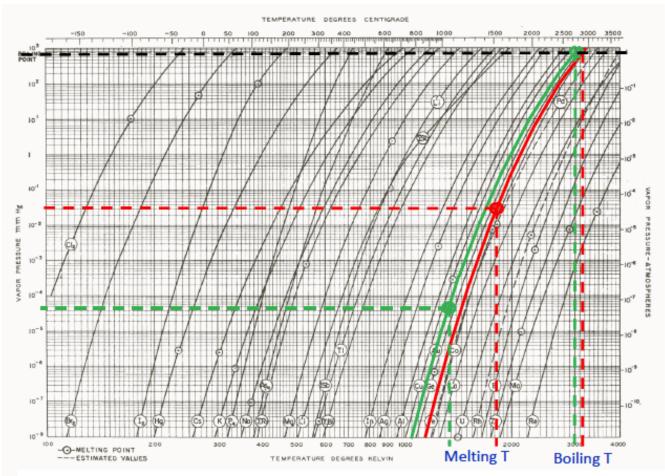


(from Lund Instrument Engineering - https://www.powerstream.com/vapor-pressure.htm)



Testo piè di pagina

Vapor pressure (3)



Vapor pressures of the more common elements. Dots represent the melting points. The intercept with the horizontal dashed line correspond to the boling points, (from Lund Instrument Engineering - https://www.powerstream.com/vapor-pressure.htm)

Ex. Fe: T melting \approx 1850 K @ $P \approx 3 \cdot 10^{-2}$ torr T boiling \approx 3100 K @ P = 1 atm

Ex. Au: $T \text{ melting} \approx 1350 \text{ K } @ P \approx 5.10^{-5} \text{ torr}$ $T \text{ boiling} \approx 3000 \text{ K } @ P = 1 \text{ atm}$

Element	Melting point (K)		
Mg	920		
Al	930		
Si	1684		
Cr	2177		
Mn	1516		
Fe	1808		
Co	1765		
Ni	1725		
Cu	1355		
Pd	1825		
Ag	1232		
Pt	2038		
Au	1334		

From oxford-vacuum.com



Testo piè di pagina 33

Vapor pressure (4)

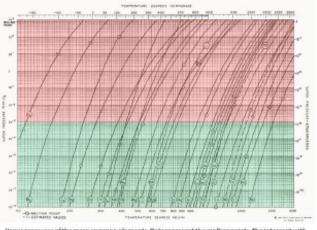
Which is the criterion for discerning between evaporation from a solid or a liquid?

The vapor pressure needed to deposit with reasonably large rate (Γ_e and ϕ_e are proportional to P_e) effectively emanates from a solid or a liquid source?

«Rule of thumb»: a melt will be required if the vapor pressure at the melting point is lower than about 10-3 torr.

Ex. Fe: at the melting point $P \approx 3.10^{-2}$ torr \Rightarrow no melting \Rightarrow Fe sublimes from the solid phase (as well as Cr, Ti, Mo, Ni, Si, ...)

Ex. Au: at the melting point $P \approx 5 \cdot 10^{-5}$ torr \Rightarrow melting \Rightarrow Au deposition is attained only when the source is molten (as well as Ge, Na, Cs, ..)



Vapor pressures of the more common elements. Dots represent the melting points. The intercept with the horizontal dashed line correspond to the boiling points, (from Lund Instrument Engineering https://www.powerstreem.com/vapor-pressure.html



Evaporation rate: example

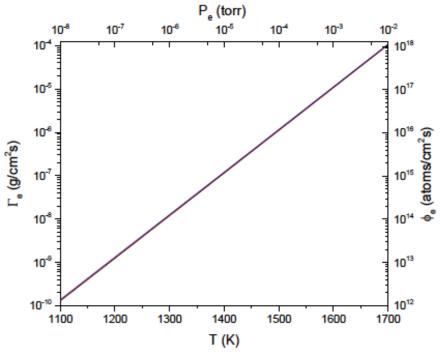
Fe deposition by thermal evaporation

- from slide 10 we extract the P_e(T) curve
- we evaluate (using M=55.84 g) the evaporation rates:

$$\Gamma_e(g/cm^2s) = \phi_e \frac{M}{N_A} = 5.84 \cdot 10^{-2} \left(\frac{M}{T}\right)^{1/2} P_e(torr)$$

$$\phi_e(atoms/cm^2s) = 3.513 \cdot 10^{22} \frac{P_e(torr)}{(MT)^{1/2}}$$

(note that the influence of the temperature T is mainly via P_e and not via the $T^{-1/2}$ dependence)



Which is the rate in terms of monolayer per second?

1 ML corresponds to about 10¹⁵ atoms/cm² (see lecture 2) $\Longrightarrow r(ML/s) = \frac{\phi_e(\text{atoms/cm}^2\text{s})}{10^{15}(\text{atoms/cm}^2)} = 3.513 \cdot 10^7 \frac{P_e(\text{torr})}{(MT)^{1/2}}$

Which is the time needed for 1 ML coverage?

$$- t_{1ML}(s) = \frac{1}{r} = 2.85 \cdot 10^{-8} \frac{(MT)^{1/2}}{P_e(\text{torr})}$$

Es.:
$$T = 1400 \text{ K} \Rightarrow r = 1.25 \text{ ML/s}, t_{1ML} = 0.8 \text{ s}$$

 $T = 1200 \text{ K} \Rightarrow r = 0.014 \text{ ML/s} = 0.84 \text{ ML/min} = 0.73.7 \text{ s}$



Evaporation of multielement materials(1)

- Metals: they evaporate as atoms or clusters of atoms

- Compounds: the vapor composition is usually different from that of the liquid/solid source stoichiometry is generally not preserved



both molecular association and dissociation can occur

Reaction type	Chemical reaction	Examples	Comments
Evaporation without dissociation	$MX(s,l) \to MX(v)$	SiO, GeO, MgO, CaF ₂	Compound stoichiometry is maintained
Evaporation with dissociation (g + g)			Deposited films are metal-rich
a) Chalcogenides	$MX(s) \rightarrow M(g)+X(g)$	CdS, CdSe, CdTe	Separate sources usually required
b) Oxides	$MO_2(s) \rightarrow MO(g)+1/2O_2(g)$	SiO ₂ , GeO ₂ , TiO ₂	Dioxides (and other complex oxides with larger oxidation number) are better deposited in O ₂ partial pressure (reactive evaporation)
Decomposition (s/l + g)	$MX(s) \rightarrow M(s)+X(g)$ $MX(s) \rightarrow M(I)+X(g)$	III-V semiconductors (GaAs, InAs)	Separate sources required



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Evaporation of multielement materials(2)

How to evaporate metal alloy films (e.g. Fe-Ni, Ni-Cr, Al-Cu) preserving the stoichiometry?

- Atoms in metallic alloys are less tightly bound than in oxides ⇒ they tend to evaporate separately (as in III-V semiconductors) ⇒ they
 enter the vapor phase as single atoms (as if they were pure metals)
- We assume that the interaction energy between A and B atoms of an AB alloy is the same for any pair (AA, BB and AB)
- The Raoult law holds: $\begin{cases} P_{\!\scriptscriptstyle A} = X_{\!\scriptscriptstyle A} P_{\!\scriptscriptstyle A0} \\ P_{\!\scriptscriptstyle B} = X_{\!\scriptscriptstyle B} P_{\!\scriptscriptstyle B0} \end{cases}$

(P_A is the **vapor pressure** of A in solution, P_{A0} is the vapor pressure of pure A, X_A is the **mole fraction** of A in the solution; the same for B; $X_A + X_B = 1$)

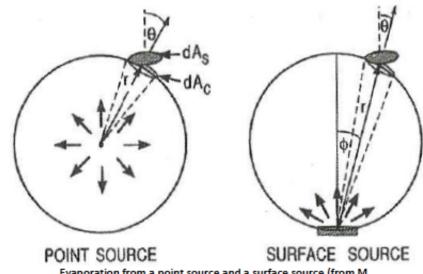
- In real situations, the mole fraction X must be replaced by the **activity** a that is the *effective* concentration of the material in the solution, taking into account the *different* evaporation rates from the solution (AB) or the pure materials (AA, BB).
- The activity can be related to the concentration by the activity coefficient $\gamma: a = \gamma X \Rightarrow \begin{cases} P_A = \gamma_A X_A P_{A0} \\ P_B = \gamma_B X_B P_{B0} \end{cases}$
- Because the evaporation flux ϕ_e is proportional to P_e/\sqrt{M} (see slide 7), at a fixed T, finally we have $\frac{\phi_A}{\phi_B} = \frac{\gamma_A X_A P_{A0}}{\gamma_B X_B P_{B0}} \left(\frac{M_B}{M_A}\right)^{1/2}$ (with $X_A + X_B = 1$)
- However, during time the source composition, and that of the vapor by consequence, evolves (because of the loss of the more volatile component) ⇒ if the fluxes are not compensated, a graded film of varying composition is deposited (disadvantage of evaporation methods!)

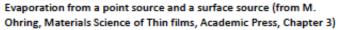


Deposition geometry (1)

Which is the film uniformity that can be obtained by a given source?

- Film uniformity depends on the source substrate geometry (orientation, placement, distance, ...)
- The basic geometries are
 - point source evaporant particles originate from an infinitesimally small region of a spherical source
 - surface source evaporant particles originate from an extended area that can be considered a superposition of many point sources







Deposition geometry (2)

- Point source evaporant particles originate from an infinitesimally small region (dA_e) of a spherical (point) source of surface area A_e with a uniform mass evaporation rate Γ_e ; the substrate (S) is at distance r from the point source
- The total evaporated mass M_e is given by $M_e = \int_0^t \int_{A_e} \Gamma_e dA_e dt$
- The mass dM_S deposited on the substrate will fall on the portion of substrate of area dA_S , whose projected area on surface of a sphere of radius r is $dA_C = dA_S \cos \theta$, where θ is the angle between the point source–substrate vector and the normal to the substrate surface.
- The following proportionality applies, assuming that the total evaporated mass is fully deposited on the sphere of area r:

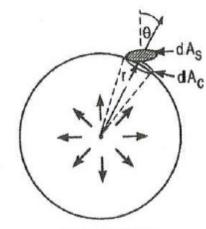
$$\frac{dM_{S}}{dA_{C}} = \frac{M_{e}}{4\pi r^{2}}$$

⇒ the mass deposited per unit area finally is

$$\frac{dM_S}{dA_C} = \frac{M_e}{4\pi r^2} \Rightarrow \frac{dM_S}{dA_S} = \frac{M_e \cos \theta}{4\pi r^2}$$

Note that deposition varies as i) 1/r² (the source-substrate distance)

ii) $\cos \theta$ (the geometric orientation of the substrate)



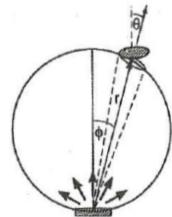
POINT SOURCE

Evaporation from a point source (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 3)

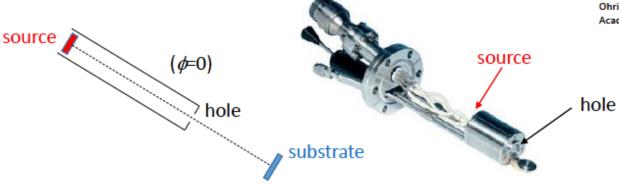


Deposition geometry (3)

- Surface source it can be considered a superposition of point sources; their contribution to the vapor stream is stronger where
 the evaporant emission angle φ (the angle between the surface source normal and the substrate) is near zero.
- The mass deposited per unit area is now dependent on angle ϕ : $\frac{dM_S}{dA_S} = \frac{M_e \cos \phi \cos \theta}{\pi r^2}$ (Note that in the ϕ =90° direction there is no emission)
- Knudsen cell source it makes use of an isothermal enclosure with a small hole through which the
 evaporant atoms or molecules will diffuse ⇒ it follows the same equation as above (with the cosine
 dependence on angle φ)



SURFACE SOURCE
Evaporation from a surface source (from M.
Ohring, Materials Science of Thin films,
Academic Press, Chapter 3)

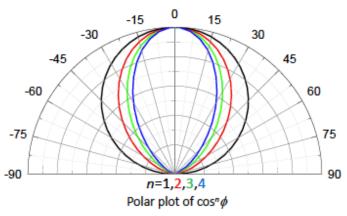


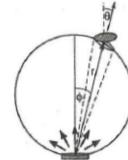
Deposition geometry (4)

- Practically, the angular distribution of the evaporant flux depends on many parameters (as the evaporation crucible geometry)
- \Rightarrow a $\cos^n \phi$ dependence has been experimentally found to be more appropriated
- n determines the the shape of the vapor cloud and the angular distribution (versus ϕ) of evaporant flux from the source
- n scales as the ratio between the depth and the surface area of the molten source material \Rightarrow narrower crucible have larger n (they are used to confine the evaporated material to a narrow angular spread)
- The mass deposited per unit area is now $\frac{dM_s}{dM_s} = \frac{M_s(n+1)\cos^n\phi\cos\theta}{2}$

$$\frac{dM_s}{dA_s} = \frac{M_s(n+1)\cos^n\phi\cos\theta}{2\pi r^2}$$

Note: because of the increased directionality of the source, the receiving suface area scales down as





Evaporation from a surface source or Kundsen cell (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 3)

Film thickness uniformity (5)

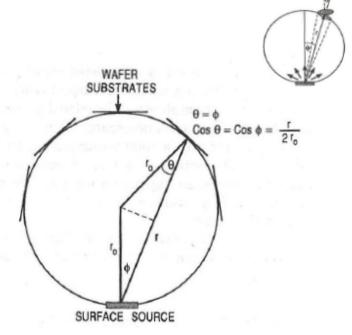
How to achieve maximum thickness uniformity on many substrates at the same time?

Both the surface sources and the substrates must be placed tangent to the surface of a sphere

$$\Rightarrow \theta = \phi \Rightarrow \cos \theta = \cos \phi = (r/2)/r_0 \Rightarrow \frac{dM_s}{dA_s} = \frac{M_e \cos \phi \cos \theta}{\pi r^2} = \frac{M_e}{\pi r^2} \frac{r}{2r_0} \frac{r}{2r_0} = \frac{M_e}{4\pi r_0^2}$$

Notes:

- the deposit thickness is independent on angle.
- This works with surface sources (n=1), but fails with more directional ones (n>1)



Evaporation scheme to achieve uniform deposition (from M. Ohring, Materials Science of Thin films, Academic Press, Chapter 3)

